# Acid-Base (Proton-Transfer) Reactions 

## Chapter 17

## An example of equilibrium: Acid base chemistry

- What are acids and bases?
- "Every day" descriptions
- Chemical description of acidic and basic solutions by Arrhenius
- Molecules as acids (proton donors) or bases (proton acceptors) - Brønsted-Lowry Acid-Base Theory
- How do they work?
- Conjugate acid-base pairs
- Strength and weakness
- Acid base equilibrium reactions: predicting favored direction
- The water equilibrium
- pH and pOH
- Calculating the equilibrium constant from pH
- Buffer solutions


## What are acids and bases?

- Historical Classifications:
- Acid: Something with a sour, biting taste (latin: acidus = sour)
- lemon juice (citric acid)
- vinegar (ethanoic acid or acetic acid)
- Base: Something that will neutralize an acid (arabic: alkali = "from the ashes")
- many medicines


## What are acids and bases?

- Svante Arrhenius (1859-1927)
- Nobel Prize, Chemistry, 1903

- The properties of an acidic solution are due to the presence of the $\mathrm{H}^{+}(\mathrm{aq})$ ion
- An acid is therefore a solution with a relatively high $\left[\mathrm{H}^{+}\right]$(square brackets = "concentration of")
- The properties of a basic solution are due to the presence of the $\mathrm{OH}^{-}(\mathrm{aq})$ ion
- A base is therefore a solution with a relatively high [ $\mathrm{OH}^{-}$]


## Arrhenius definition of acidic and basic solutions

- An Arrhenius acid
- solution with a relatively high $\left[\mathrm{H}^{+}\right]$
$\mathrm{HCl}(\mathrm{g}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}(\mathrm{l})} \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})$
- An Arrhenius base
- solution with a relatively high [ $\mathrm{OH}^{-}$]


$$
\mathrm{NaOH}(\mathrm{~s}) \xrightarrow{\mathrm{H}_{2} \mathrm{O}(\mathrm{l})} \mathrm{Na}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})
$$

## Brønsted-Lowry Acid-Base Theory

- An acid-base reaction is a proton-transfer reaction
- Acid: proton donor
- Base: proton acceptor



## Proton-transfer reaction



## Acids and bases appear in pairs

- For every proton donor on the reactant side you need a proton acceptor on the product side!
Base: proton acceptor
Acid: proton donor
Acid: proton
donor

Base: proton acceptor
$\mathrm{NH}_{3}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\ell) \rightleftharpoons \mathrm{NH}_{4}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$


- Where does the equilibrium lie?
- In $1 \mathrm{M} \mathrm{NH}_{3}(\mathrm{aq})$ less than $1 \%$ of the ammonia becomes ammonium ions
- $\mathrm{NH}_{3}$ is the major species, the reverse reaction is favored


## Acids and bases appear in pairs

- For every proton donor you need a proton acceptor!

- B and $\mathrm{HB}^{+}$differ by a proton:
- They form a conjugate acid-base pair
- Similarly, HA and A $^{-}$are a conjugate acid-base pair



## Water is (again) remarkable

$$
\mathrm{HNO}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{NO}_{3}^{-}(\mathrm{aq})+\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})
$$

Base $=$ Proton Acceptor: $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$

$$
\mathrm{NH}_{3}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \rightleftharpoons \mathrm{NH}_{4}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})
$$

Acid $=$ Proton Donor: $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$
Water is an acid in one case and a base in another

Amphoteric: A species that can behave as either an acid or a base

## Strong and weak acids

Question: What determines the position of the equilibrium?
Answer: The strengths of the acid and base

- Strong acids are (almost) completely ionized:
- $\mathrm{HSt}(\mathrm{aq}) \longrightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{St}^{-}(\mathrm{aq})$
- They are better proton donors
- Weak acids are not ionized:
- $\mathrm{HWk}(\mathrm{aq}) \longrightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Wk}^{-}(\mathrm{aq})$
- They do not as readily donate protons


## Strong and weak acids

Stronger acids


Weaker acids

More ionized


Less ionized

Strong acid = better proton donor
$\mathrm{HCl}(\mathrm{aq})$, hydrochloric acid, is a stronger acid:
It is a good proton donor

$$
\mathrm{HCl}(\mathrm{aq}) \rightleftharpoons \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})
$$

Now consider the reaction in the reverse direction:
How good is $\mathrm{Cl}^{-}(\mathrm{aq})$ as a base?
$\mathrm{HCl}(\mathrm{aq}) \quad \hookleftarrow \quad \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})$
Chloride ion is a relatively poor proton acceptor
Therefore it is a weaker base

$\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2} \mathrm{H}(\mathrm{aq})$, acetic acid, is a weaker acid:
It is a poor proton donor
$\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2} \mathrm{H}(\mathrm{aq}) \quad \Rightarrow \quad \mathrm{H}^{+}(\mathrm{aq})+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}(\mathrm{aq})$

Now consider the reaction in the reverse direction:
How good is $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}{ }^{-}(\mathrm{aq})$ as a base?
$\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2} \mathrm{H}(\mathrm{aq}) \longleftarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}(\mathrm{aq})$
The $\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}(\mathrm{aq})$ ion has a strong attraction for protons It is a strong base


## Strong and weak: summary

- Stronger acid = weaker conjugate base
- The conjugate base is poor at accepting a proton
- The acid is good at donating a proton
- The species prefers to be de-protonated!
$\mathrm{HCl}(\mathrm{aq}) \rightleftharpoons \mathrm{H}^{+}(\mathrm{aq})+\mathrm{Cl}^{-}(\mathrm{aq})$
- Weak acid = stronger conjugate base
- The conjugate base is good at accepting a proton
- The acid is poor at donating a proton
- The species prefers to be protonated!

$$
\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2} \mathrm{H}(\mathrm{aq}) \rightleftharpoons \mathrm{H}^{+}(\mathrm{aq})+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}(\mathrm{aq})
$$



## Reactivity of acids

- Most acid-base reactions are reversible. Can we predict which will be present in greater concentration at equilibrium : reactants or products?
- A stronger acid is good at donating protons: It is relatively reactive
- A stronger base is good at accepting protons: It is relatively reactive
- A weaker acid is a poor proton donor: It is relatively inert
- A weaker base is a poor proton acceptor: It is relatively inert


## Reactivity of acids

- It's all about the conjugate base!
- If the CB has available electrons (-) it will hold a proton (+) tightly - strong conjugate base, weak acid (eg acetic acid)
- If the CB has a noble gas configuration, electrons are not available for bonding and the proton is not held tightly - weak conjugate base, strong acid (eg HCl)


## Proton-transfer reactions at equilibrium:

- The stronger acid will transfer a proton to the stronger base, yielding the weaker acid and weaker base as favored species at equilibrium
$\mathrm{HA}+\mathrm{B} \longrightarrow \mathrm{A}^{-}+\mathrm{HB}^{+}$
Strong acid: Strong base: Weak base: Weak acid: good proton good proton poor proton poor proton donor acceptor acceptor donor


## Example

- Write the equation for the reaction between hydrogen sulfate ion and hydroxide ion.
- Predict which side will be favored at equilibrium.

Step 1: Write the equation for the proton transfer

$$
\mathrm{HSO}_{4}^{-}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \rightleftharpoons \mathrm{SO}_{4}{ }^{2-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{I})
$$

Step 2: Label acids and bases
$\underset{\text { Acid }}{\mathrm{HSO}_{4}^{-}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})} \underset{\text { Base }}{\sim} \underset{\text { Base }}{\mathrm{SO}_{4}{ }^{2-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l})}$


## Example

|  | Acids: $\mathrm{HSO}_{4}{ }^{-}(\mathrm{aq})>\mathrm{H}_{2} \mathrm{O}(\mathrm{l})$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Bases: $\mathrm{SO}_{4}{ }^{2-}(\mathrm{aq})<\mathrm{OH}^{-}(\mathrm{aq})$ |  |  |  |  |
| $\mathrm{HSO}_{4}^{-}(\mathrm{aq})$ | $+\mathrm{OH}^{-}(\mathrm{aq})$ | $\mathrm{SO}_{4}{ }^{2-}(\mathrm{aq})$ |  | $\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$ |
| Stronger acid | Stronger base | Weaker base |  | Weaker acid |

Reaction is favored in the forward direction

## Chalkboard example

- For the following acids and bases complete the proton transfer equation and predict the direction in which the resulting equilibrium will be favored
$\mathrm{NH}_{4}{ }^{+}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{BO}_{3}^{-}(\mathrm{aq})$
$\mathrm{NO}_{2}^{-}(\mathrm{aq})+\mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})$

| Hydroiodic |  | Hi | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{I}^{-}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Hydrobromic |  | HBr | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{Br}^{-}$ |  |
| Perchloric |  | $\mathrm{HClO}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{ClO}_{4}^{-}$ |  |
| Hydrochloric |  | HCl | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{Cl}^{-}$ |  |
| Sulfuric |  | $\mathrm{H}_{2} \mathrm{SO}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HSO}_{4}^{-}$ |  |
| Chloric |  | $\mathrm{HClO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{ClO}_{3}^{-}$ |  |
| Nitric |  | $\mathrm{HNO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{NO}_{3}^{-}$ |  |
| Hydronium ion |  | $\mathrm{H}_{3} \mathrm{O}^{+}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{H}_{2} \mathrm{O}$ |  |
| Oxalic |  | $\mathrm{H}_{2} \mathrm{C}_{2} \mathrm{O}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HC}_{2} \mathrm{O}_{4}^{-}$ |  |
| Sulfurous |  | $\mathrm{H}_{2} \mathrm{SO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HSO}_{3}^{-}$ |  |
| Hydrogen sulfate ion |  | $\mathrm{HSO}_{4}^{-}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{SO}_{4}{ }^{-}$ |  |
| Phosphoric | $0$ | $\mathrm{H}_{3} \mathrm{PO}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$ |  |
| Hydrofluoric | $\frac{\cdot}{\omega}$ | HF | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{F}^{-}$ | $\stackrel{\omega}{\infty}$ |
| Nitrous | $\mathscr{N}$ | $\mathrm{HNO}_{2}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{NO}_{2}^{-}$ | $\stackrel{\omega}{\sigma}$ |
| Formic (methanoic) | ㅡㅡㄷ | $\mathrm{HCHO}_{2}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{CHO}_{2}^{-}$ | $0$ |
| Benzoic | $\frac{=}{5}$ | $\mathrm{HC}_{7} \mathrm{H}_{5} \mathrm{O}_{2}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{O}_{2}^{-}$ | $\stackrel{\rightharpoonup}{5}$ |
| Hydrogen oxalate ion | $\stackrel{5}{\circ}$ | $\mathrm{HC}_{2} \mathrm{O}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{C}_{2} \mathrm{O}_{4}{ }^{2-}$ | 亏ू |
| Acetic (ethanoic) | © | $\mathrm{HC}_{2} \mathrm{H}_{3} \mathrm{O}_{2}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{O}_{2}^{-}$ | థ |
| Propionic (propanoic) | ぁ | $\mathrm{HC}_{3} \mathrm{H}_{5} \mathrm{O}_{2}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{C}_{3} \mathrm{H}_{5} \mathrm{O}_{2}^{-}$ |  |
| Carbonic | $\frac{0}{0}$ | $\mathrm{H}_{2} \mathrm{CO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HCO}_{3}^{-}$ | $\bigcirc$ |
| Hydrosulfuric | 4 | $\mathrm{H}_{2} \mathrm{~S}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HS}^{-}$ |  |
| Dihydrogen phosphate ion |  | $\mathrm{H}_{2} \mathrm{PO}_{4}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{HPO}_{4}{ }^{2-}$ |  |
| Hydrogen sulfite ion |  | $\mathrm{HSO}_{3}{ }^{-}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{SO}_{3}{ }^{2-}$ |  |
| Hypochlorous |  | HClO | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{ClO}^{-}$ |  |
| Boric |  | $\mathrm{H}_{3} \mathrm{BO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{H}_{2} \mathrm{BO}_{3}^{-}$ |  |
| Ammonium ion |  | $\mathrm{NH}_{4}{ }^{+}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{NH}_{3}$ |  |
| Hydrocyanic |  | HCN | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{CN}^{-}$ |  |
| Hydrogen carbonate ion |  | $\mathrm{HCO}_{3}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{CO}_{3}^{2}$ |  |
| Monohydrogen phosphate ion |  | $\mathrm{HPO}_{4}{ }^{2-}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{PO}_{4}{ }^{3-}$ |  |
| Hydrogen sulfide ion |  | $\mathrm{HS}^{-}$ | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{S}^{2-}$ |  |
| Water |  | HOH | $\rightleftharpoons \mathrm{H}^{+}+\mathrm{OH}^{-}$ |  |

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## The water equilibrium

- Autoionization of water

$$
\begin{aligned}
& \mathrm{H}_{2} \mathrm{O}(\mathrm{I})+\mathrm{H}_{2} \mathrm{O}(\mathrm{I}) \\
& \Rightarrow \\
& \mathrm{H}_{3} \mathrm{O}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq}) \\
& \mathrm{H}_{2} \mathrm{O}(\mathrm{I}) \\
& \Longleftrightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})
\end{aligned}
$$

## The water equilibrium

$$
\mathrm{H}_{2} \mathrm{O}(\mathrm{l})<\mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})
$$

- For pure water at $25^{\circ} \mathrm{C},\left[\mathrm{H}^{+}\right]=1.0 \times 10^{-7} \mathrm{M}$ (this is a measured quantity)
- Every $\mathrm{H}_{2} \mathrm{O}$ that breaks apart creates one $\mathrm{OH}^{-}$and one $\mathrm{H}^{+}$
- So $\left[\mathrm{OH}^{-}\right]=\left[\mathrm{H}^{+}\right]$in pure water
- $\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$
- Thinking like a chemist: one in ten million H-bonded water molecules give their proton to another $\mathrm{H}_{2} \mathrm{O}$

$$
\begin{aligned}
& \text { The water equilibrium } \\
& \mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \quad \Longleftrightarrow \mathrm{H}^{+}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})
\end{aligned}
$$

- In pure water, $\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$

$$
\begin{aligned}
& \text { Equilibrium constant }=\mathrm{K}_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right] \\
& =\left(1.0 \times 10^{-7}\right) \times\left(1.0 \times 10^{-7}\right)=1.0 \times 10^{-14}
\end{aligned}
$$

## What are acids and bases?

- An aqueous solution is said to be neutral if $\left[\mathrm{H}^{+}\right]=$ [ $\mathrm{OH}^{-}$]

For pure water at $25^{\circ} \mathrm{C}$,
$\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-7} \mathrm{M}$

- If $\left[\mathrm{H}^{+}\right]>\left[\mathrm{OH}^{-}\right]$, a solution is acidic

$$
\left[\mathrm{H}^{+}\right]>1.0 \times 10^{-7} \mathrm{M} \text { and }
$$

$\left[\mathrm{OH}^{-}\right]<1.0 \times 10^{-7} \mathrm{M}$

- If $\left[\mathrm{OH}^{-}\right]>\left[\mathrm{H}^{+}\right]$, a solution is basic

$$
\left[\mathrm{OH}^{-}\right]>1.0 \times 10^{-7} \mathrm{M} \text { and }
$$

$\left[\mathrm{H}^{+}\right]<1.0 \times 10^{-7} \mathrm{M}$

## Example

- What is the hydrogen ion concentration in a solution in which the hydroxide ion concentration is $10^{-4} \mathrm{M}$ ?
- Is the solution acidic or basic?

GIVEN: $\left[\mathrm{OH}^{-}\right]=10^{-4} \mathrm{M} \quad$ WANTED: $\left[\mathrm{H}^{+}\right]$

$$
\text { EQUATION: } \mathrm{K}_{\mathrm{w}}=\left[\mathrm{H}^{+}\right]\left[\mathrm{OH}^{-}\right]=1.0 \times 10^{-14}
$$

$$
\left[\mathrm{H}^{+}\right]=\frac{\mathrm{K}_{\mathrm{w}}}{\left[\mathrm{OH}^{-}\right]}=\frac{10^{-14}}{10^{-4}}=10^{-10}
$$

Since $\left[\mathrm{H}^{+}\right]=10^{-10}<\left[\mathrm{OH}^{-}\right]=10^{-4}$, the solution is basic

## A touch of math here:

- Multiplying numbers in exponential notation: add the powers
$\left(1.0 \times 10^{-7}\right) \times\left(1.0 \times 10^{-7}\right)=1.0 \times 10^{-14}$
- simple demonstration:
$2^{3} \times 2^{5}=(2 \times 2 \times 2) \times(2 \times 2 \times 2 \times 2 \times 2)=2^{8}$
- Division: subtract the powers
$\left(1.0 \times 10^{-28}\right) \times\left(1.0 \times 10^{-21}\right)=1.0 \times 10^{-7}$
- simple demonstration:

$$
2^{5} / 2^{3}=\frac{(2 \times 2 \times 2 \times 2 \times 2)}{(2 \times 2 \times 2)}=2^{2}
$$

## Logarithms or logs

- The logarithms of a number to a given base is the power or exponent to which the base must be raised in order to produce the number
- if $x=b^{y}$ then $y=\log _{b}(x)$
- $\log _{10}\left(1 \times 10^{7}\right)$ is 7
- $\log _{10}\left(1 \times 10^{8}\right)$ is 8
- $\log _{10}\left(6.2 \times 10^{7}\right)$ is 7.79



## Logarithms or logs

$\log _{10}\left(1 \times 10^{-7}\right)$ is -7
$\log _{10}(0.0001)$ is -4
$\log _{10}(0.00001)$ is -5
$\log _{10}(0.00002)$ is -4.699

Play with the log button on your calculator until this starts to make sense

## Why use logarithms?

- Multiplying very large or very small numbers was extremely difficult before the advent of calculators
- It is much more convenient for numbers that have large powers of 10
- For example: concentrations of $\left[\mathrm{H}^{+}\right]$and $\left[\mathrm{OH}^{-}\right]$!


## The p function

- $p$ is math short-hand for ' $-1 \times \log _{10}$ '

Applied to $\left[\mathrm{H}^{+}\right]$and $\left[\mathrm{OH}^{-}\right]$,
$\mathrm{pH}=-\log _{10}\left[\mathrm{H}^{+}\right]$
$\mathrm{pOH}=-\log _{10}\left[\mathrm{OH}^{-}\right]$

In pure water, $\left[\mathrm{H}^{+}\right]=\left[\mathrm{OH}^{-}\right]=10^{-7} \mathrm{M}$

$$
\mathrm{pH}=\mathrm{pOH}=-\log _{10}\left(10^{-7}\right)=7
$$

## pH and pOH

- An aqueous solution is neutral if $\left[\mathrm{H}^{+}\right]=10^{-7} \mathrm{M}$
- A solution is acidic if $\left[\mathrm{H}^{+}\right]>10^{-7} \mathrm{M}$
- A solution is basic if $\left[\mathrm{H}^{+}\right]<10^{-7} \mathrm{M}$
- Translating concentrations to pH 's:
- Neutral: $\mathrm{pH}=7$
- Acidic: $\mathrm{pH}<7$
- Basic: pH > 7



## Example

- The hydrogen ion concentration of a solution is 2.7 x $10^{-6} \mathrm{M}$.
- What are the $\mathrm{pH}, \mathrm{pOH}$, and hydroxide ion concentration?

$$
\begin{gathered}
\mathrm{pH}=-\log _{10}\left[\mathrm{H}^{+}\right]=-\log _{10}\left(2.7 \times 10^{-6}\right)=5.57 \\
\mathrm{pH}+\mathrm{pOH}=14 \\
\mathrm{pOH}=14.00-\mathrm{pH}=14.00-5.57=8.43 \\
{\left[\mathrm{OH}^{-}\right]=10(-\mathrm{pOH})=} \\
10^{(-8.43)}=3.7 \times 10^{-9} \mathrm{M}
\end{gathered}
$$

## Working with pH and pOH



The pH Loop
Given the value for any corner of the loop, all other values may be calculated by progressing round the loop (in either direction)

## Interpreting pH Values

| $\left[\mathbf{H}^{+}\right]$ | $\left[\mathbf{H}^{+}\right]$ | $\mathbf{p H}$ | Acidity or Basicity ${ }^{*}$ |
| :--- | :---: | :---: | :---: |
| 1.0 | $10^{0}$ | 0 |  |
| 0.1 | $10^{-1}$ | 1 |  |
| 0.01 | $10^{-2}$ | 2 | Strongly acid |
| 0.001 | $10^{-3}$ | 3 | $\mathrm{pH}<4$ |
| 0.0001 | $10^{-4}$ | 4 |  |
| 0.0001 | $10^{-4}$ | 4 |  |
| 0.00001 | $10^{-5}$ | 5 | Weakly acid |
| 0.000001 | $10^{-6}$ | 6 | $4 \leq \mathrm{pH}<6$ |
| 0.000001 | $10^{-6}$ | 6 | Neutral |
| 0.0000001 | $10^{-7}$ | 7 | (or near neutral) |
| 0.00000001 | $10^{-8}$ | 8 | $6 \leq \mathrm{pH}<8$ |
| 0.00000001 | $10^{-8}$ | 8 |  |
| 0.000000001 | $10^{-9}$ | 9 | Weakly basic |
| 0.0000000001 | $10^{-10}$ | 10 | $8 \leq \mathrm{pH}<10$ |
| 0.0000000001 | $10^{-10}$ | 10 |  |
| 0.00000000001 | $10^{-11}$ | 11 |  |
| 0.000000000001 | $10^{-12}$ | 12 | Strongly basic |
| 0.0000000000001 | $10^{-13}$ | 13 | $10 \leq \mathrm{pH}$ |
| 0.00000000000001 | $10^{-14}$ | 14 |  |



## Calculating $\mathrm{K}_{\mathrm{a}}$, the equilibrium constant, for weak acids

- Strong acids can be assumed to be completely dissociated
- For weak acids ( $\mathrm{K}_{\mathrm{a}}$ between $1 \times 10^{-3}$ and $1 \times 10^{-13}$ ) the equilibrium constant can be estimated from the pH of a known concentration

$$
\begin{aligned}
& \mathrm{HA}(\mathrm{aq}) \rightleftharpoons \mathrm{H}^{+}(\mathrm{aq})+\mathrm{A}^{-}(\mathrm{aq}) \\
& \mathrm{pH}=-\log \left[\mathrm{H}^{+}\right], \quad \text { so }\left[\mathrm{H}^{+}\right]=10-\mathrm{pH} \\
& \mathrm{~K}_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{A}^{-}\right]}{[\mathrm{HA}]}
\end{aligned}
$$

## Example

Calculate the $\mathrm{K}_{\mathrm{a}}$ for benzoic acid $\left(\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right)$.
When 4.2 g of benzoic acid are dissolved in 1 L of water the pH is 2.84

1) Write the equation and the equilibrium constant expression

$$
\begin{gathered}
\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H} \rightleftharpoons \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}^{--}+\mathrm{H}^{+} \\
\mathrm{Ka}=\frac{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}^{-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right]}
\end{gathered}
$$

2) Determine the relative concentrations of the species

The total concentration of benzoic acid is:

$$
\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right]=\frac{4.2 \mathrm{~g} \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}}{122 \mathrm{~g} \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}}=0.034 \mathrm{M}
$$

The concentration of dissociated benzoic acid is:
$\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}{ }^{-}\right]=\left[\mathrm{H}^{+}\right]=10^{-\mathrm{pH}}=10^{-2.84}=1.45 \times 10^{-3} \mathrm{M}$
Less than $5 \%$ of the benzoic acid is deprotonated = weak acid
3) Plug these numbers back into the $K_{a}$ expression

$$
\mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}^{-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right]}=\frac{\left(1.45 \times 10^{-3}\right)\left(1.45 \times 10^{-3}\right)}{0.034}
$$

$$
K_{a}=6.2 \times 10^{-5}
$$

Notice that we have assumed that all the acid is undissociated.
If we solve correctly it doesn't make much difference for weak acids:

$$
\begin{aligned}
\mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2}^{-}\right]\left[\mathrm{H}^{+}\right]}{\left[\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{CO}_{2} \mathrm{H}\right]} & =\frac{\left(1.45 \times 10^{-3}\right)\left(1.45 \times 10^{-3}\right)}{\left(0.034-1.45 \times 10^{-3}\right)} \\
\mathrm{K}_{\mathrm{a}} & =6.5 \times 10^{-5}
\end{aligned}
$$

## Buffer solutions

- A buffer solution is an aqueous solution consisting of a mixture of a weak acid and its conjugate base or a weak base and its conjugate acid.
- It has the property that the pH of the solution changes very little when a small amount of acid or base is added to it.
- Add base: it is neutralized by (reacts with) the acid
- Add acid: it is neutralized by (reacts with) the base
- Buffer solutions are used as a means of keeping pH at a nearly constant value in a wide variety of chemical applications.


## Buffer solutions

- In a buffer solution there is an equilibrium between a weak acid, HA, and its conjugate base, A-

$$
\mathrm{HA} \rightleftharpoons \mathrm{H}^{+} \quad+\mathrm{A}^{-}
$$

- When hydrogen ions are added to the solution the equilibrium moves to the left, in accordance with Le Chatelier's principle
- When hydroxide ions are added the equilibrium moves to the right as hydrogen ions are removed in the reaction

$$
\mathrm{H}^{+}+\mathrm{OH}^{-} \rightleftharpoons \mathrm{H}_{2} \mathrm{O}
$$

- Some of the added material is consumed in shifting the equilibrium and the pH changes by less than it would do if the solution were not buffered.

$$
\begin{aligned}
& \text { Example: the } \mathrm{H}_{2} \mathrm{PO}_{4}-/ \mathrm{HPO}_{4}{ }^{2-} \\
& \text { system } \\
& \mathrm{H}_{2} \mathrm{PO}_{4}^{-}(\mathrm{aq}) \rightleftharpoons \rightleftharpoons \mathrm{H}^{+}(\mathrm{aq})+\mathrm{HPO}_{4}{ }^{2-}(\mathrm{aq}) \\
& \mathrm{K}_{\mathrm{a}}=\frac{\left[\mathrm{H}^{+}\right]\left[\mathrm{HPO}_{4}{ }^{2-}\right]}{\left[\mathrm{H}_{2} \mathrm{PO}_{4}^{-}\right]}
\end{aligned}
$$

Add acid:
$\mathrm{H}^{+}(\mathrm{aq})+\mathrm{HPO}_{4}{ }^{2-}(\mathrm{aq}) \longrightarrow \mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}(\mathrm{aq})$

Add base:
$\mathrm{OH}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{PO}_{4}{ }^{-}(\mathrm{aq}) \longrightarrow \mathrm{HPO}_{4}{ }^{2-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{I})$

